Phonon and magnetic dimer excitations in Fe-based S = 2 spin-ladder compound BaFe₂Se₂O

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Raman scattering spectra of the new Fe-based S = 2 spin-ladder compound BaFe₂Se₂O are measured in a temperature range between 15 and 623 K. All six A_{1g} and two B_{1g} Raman active modes of BaFe₂Se₂O, predicted by the factor-group analysis, have been experimentally observed at energies that are in a rather good agreement with the lattice dynamics calculation. The antiferromagnetic long-range spin ordering in BaFe₂Se₂O below $T_N = 240$ K leaves a fingerprint both in the A_{1g} and B_{1g} phonon mode linewidth and energy. In the energy range between 400 and 650 cm⁻¹ we have observed a magnetic excitation related structure in the form of a magnon continuum, with the peaks corresponding to the singularities in the one-dimensional density of magnon states. The onset value of magnetic continuum ($2\Delta_S$) is found at about 437 cm⁻¹ at 15 K. The magnetic continuum disappears at about 623 K, which led us to conclude that the short-range magnetic ordering in BaFe₂Se₂O exists apparently up to 2.6 T_N .

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I. INTRODUCTION

Iron-based superconductors are among the top priorities in physics since their discovery in 2008.¹ Within this area one of the most active fields in research are ternary alkalimetal iron selenide superconductors. The progress in this field was recently summarized in Ref. 2. While searching for new Fe-chalcogenide (S, Se, Te) compounds that are related to high-temperature superconductors in their structural and electronic properties, researchers discovered² another intriguing class of materials: the two-leg ladder selenides BaFe₂Se₃ and BaFe₂Se₂O. In fact, iron-based compounds can have not only superconducting but also low-dimensional magnetic properties^{2–4} (forming spin chains, spin ladders, spin dimers, etc.), as in the case of cuprates⁵ or vanadates.⁶ This opens up a new field of research in the direction of synthesis of new Fe-based materials, and the new physics of the S = 2quantum spin systems.⁷

BaFe₂Se₃ is an insulator with a long-range antiferromagnetic (AFM) order with T_N around 250 K and short-range AFM order at higher temperatures.^{8–10} It was shown that a dominant order involves 2 × 2 blocks of ferromagnetically aligned iron spins, whereas these blocks order antiferromagnetically, in the same manner as the block-AFM $\sqrt{5} \times \sqrt{5}$ state of the iron-vacancy-ordered A_2 Fe₄Se₅.^{11–13}

BaFe₂Se₂O belongs to the family of layered iron oxychalcogenides, which has been recently synthesized.^{3,4,14–16} Actually, this is the first layered iron oxychalcogenide with an alkali-earth element. The band structure calculations of BaFe₂Se₂O revealed⁴ the narrowing of Fe 3*d* bands near the Fermi energy, which leads to the localization of magnetism and the Mott insulating behavior. Besides the long-range AFM transition at 240 K, which is confirmed with the resistivity, specific heat, and magnetic susceptibility measurements,^{3,4} there are two additional transitions at about 115 and 42 K, where magnetic susceptibility drops abruptly.³ The magnetic entropy up to 300 K is much smaller than the expected value for Fe²⁺ in tetrahedral crystal fields, and the Mössbauer spectrum indicates that long-range magnetic order is unlikely at 294 K. Both results suggest that short-range magnetic correlations exist above room temperature.³

Barium iron oxyselenide has a unique crystal structure which is built up by stacking the Ba cations and Fe-Se(O) layers alternately along the *c* axis [Fig. 1(b)]. Within the Fe-Se(O) layers, double chains of edge-shared Fe-Se(O) tetrahedra propagate along the Se atoms parallel to the *b* axis. The Fe-Se(O) double chains are bridged by oxygen along the *a* axis [Fig. 1(a)]. The crystal structure is orthorhombic, space group *Pmmn* with two formula units (Z = 2) per unit cell.

In BaFe₂Se₂O, all iron ions are in the Fe²⁺ oxidation state and in the high spin S = 2 state.⁷ The magnetic structure of BaFe₂Se₂O may be considered as the S = 2 spin-ladder system, where the AFM exchange interaction J_1 along the rungs is dominant (strong Fe-O-Fe superexchange interaction). According to the local-spin-density-approximation (LSDA) calculations⁴ the interladder interaction J_2 is more than three times weaker than along the rungs. The exchange interaction J_3 along the ladder legs can be neglected,⁴ see Fig. 1. Because the magnetic exchange interaction is short range and the magnetic coupling farther than the second nearest neighbor is almost equal to zero, this magnetic system can be described as a two-dimensional AFM dimer system with non-negligible interdimer interaction.

In this paper we have measured polarized Raman scattering spectra of BaFe₂Se₂O in the temperature range between 15 and 623 K (350 °C). Besides the optical phonons, which are assigned using polarized measurements and the lattice dynamical calculations, we have observed a magnon continuum, which is related to the AFM dimer structure. A spin-gap value of 27 meV is obtained from the position of the onset of the magnetic continuum. High-temperature Raman scattering measurements show that the short-range magnetic order disappears at about 623 K = $2.6T_N$. In the short-range order region we have observed coupling of antiferromagnetic spin fluctuations with the B_{1g} symmetry phonons.

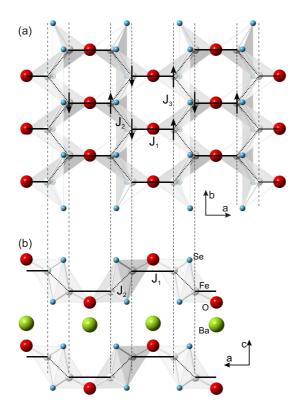


FIG. 1. (Color online) Schematic representation of $BaFe_2Se_2O$ crystal structure. (a) Fe-Se(O) layer in the (*ab*) plane. (b) the (*ac*) plane of $BaFe_2Se_2O$ crystal structure. J_1 represents the AFM Fe-O-Fe exchange interaction, J_2 is the AFM interdimer Fe-Se-Fe exchange interaction along the ladder legs. Arrows denote orientation of the magnetic moments (spins).

II. EXPERIMENT AND NUMERICAL METHOD

Single crystals of BaFe₂Se₂O were grown using the selfflux method, described in detail elsewhere.³ Raman scattering measurements were performed on (001)-oriented samples in a backscattering micro-Raman configuration. Low-temperature measurements were performed using a KONTI CryoVac continuous-flow cryostat coupled with a JY T64000 Raman system. High-temperature measurements were done using a LINKAM THMS600 heating stage coupled with the TriVista 557 Raman system. To avoid oxidation of the sample the high-temperature measurements were done in an Ar inert atmosphere. The 514.5 and 488 nm lines of an Ar⁺/Kr⁺ mixed gas laser were used as excitation sources.

The calculations are performed within the density functional theory as implemented in the QUANTUM ESPRESSO package.¹⁷ The lattice dynamics is calculated within the density functional perturbation theory¹⁸ using the projector augmented-wave method with the PBE exchange-correlation functional which is used to obtain ultrasoft pseudopotentials. The Brillouin zone is sampled with a Monkhorst-Pack $16 \times 16 \times 10$ k-space mesh. The unit cell is constructed using experimental values of the lattices parameters³ (*Pmmn* space group with unit cell parameters a = 0.98518 nm, b = 0.41332, and c = 0.67188 nm). Fractional coordinates are relaxed until all forces acting on individual atoms become smaller than 10^{-4} Ry/a.u. and they agree with experimental coordinates within a few percent. The energy cutoffs for the wave functions and the electron densities are 64 and 782 Ry, respectively, which are the highest suggested radii for the chosen pseudopotentials.

III. RESULTS AND DISCUSSION

The BaFe₂Se₂O unit cell consists of two formula units comprising 12 atoms. The site symmetries of atoms in the *Pmmn* space group are $C_{2\nu}$ (Ba, O) and C_s (Fe, Se). Factor group analysis yields

$$(C_{2v}): \Gamma = A_g + B_{2g} + B_{3g} + B_{1u} + B_{2u} + B_{3u},$$

$$(C_s): \Gamma = 2A_g + B_{1g} + 2B_{2g} + B_{3g} + A_u + 2B_{1u} + B_{2u} + 2B_{3u}.$$

Summarizing these representations and subtracting the acoustic $(B_{1u}+B_{2u}+B_{3u})$ and silent $(2A_u)$ modes, we obtained the following irreducible representations of BaFe₂Se₂O vibrational modes:

$$\Gamma_{\text{BaFe}_2\text{Se}_2\text{O}}^{\text{optical}} = 6A_g + 2B_{1g} + 6B_{2g} + 4B_{3g} + 5B_{1u} + 3B_{2u} + 5B_{3u},$$

Thus 18 Raman and 13 infrared active modes are expected to be observed in the BaFe₂Se₂O vibrational spectra. Because the crystals have the (001) orientation (the crystallographic *c* axis is perpendicular to the plane of the single crystal), we were able to obtain only the A_g and B_{1g} symmetry modes in the Raman experiment. The results of the lattice dynamics calculations, together with the experimental data, are presented in Table I. Normal modes of the A_g symmetry Raman active phonons are presented in Fig. 2.

The polarized Raman spectra of $BaFe_2Se_2O$, measured from (001) plane at room temperature and 15 K, for the parallel and crossed polarization configurations, are given in

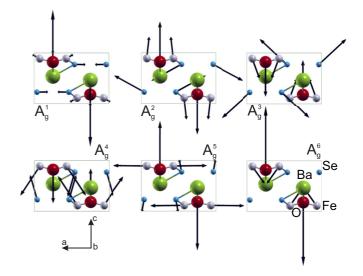


FIG. 2. (Color online) Normal modes of the A_g symmetry Raman active vibrations of BaFe₂Se₂O projected to the (*ac*) plane. The arrow lengths are proportional to the vibrational forces.

TABLE I. Calculated and experimentally observed values of Raman active phonon mode energies (in cm^{-1}) of BaFe₂Se₂O single crystal.

Raman modes					Infrared modes		
Experiment							
Symmetry	Calc.	300 K	15 K	Activity	Symmetry	Calc.	Activity
A_g^1	58.2	64	68	(xx, yy, zz)	A_u^1	66.8	Silent
	110.0	96	99.6	"	A_u^2	176.7	"
$egin{array}{c} A_g^2 \ A_g^3 \ A_g^4 \ A_g^5 \ A_g^5 \end{array}$	162.5	163	171.7	"	_	_	_
A_g^4	242.0	227	232.6	"	B_{1u}^{1}	73.4	
A_g^5	249.2	245	253	"	B_{1u}^{2}	134.2	
A_g^6	342.0	261	266.7	"	B_{1u}^{3}	229.6	E c
B_{1g}^{1}	96.7	91	93	(xy)	B_{1u}^{4}	260.8	
B_{1g}^{2}	170.4	177	181	"	B_{1u}^{5}	348.6	
B_{2g}^{1}	63.8			(xz)	-	_	-
B_{2g}^2 B_{2g}^3	106.6			"	B_{2u}^{1}	75.8	
B_{2g}^{3}	136.7			"	B_{2u}^{2}	153.2	E b
B_{2g}^4 B_{2g}^5	180.4			"	B_{2u}^{3}	232.2	
B_{2g}^{5}	255.2			"	-	_	-
B_{2g}^{6}	663.2			"	B_{3u}^{1}	50.0	
B_{3g}^{1}	58.7			(yz)	B_{3u}^{2}	113.5	
B_{3g}^{2}	88.9			"	B_{3u}^{3}	183.0	E a
B_{3g}^{3}	171.5			"	B_{3u}^{4}	281.2	
B_{3g}^4	264.1			,,	B_{3u}^{5}	662.5	

Figs. 3 and 4, respectively. The spectra measured for parallel polarization configurations consist of the A_g symmetry modes. Four modes at about 64, 96, 163, and 227 cm⁻¹ (300 K) are clearly observed for the $c(bb)\bar{c}$ polarization configuration and two additional modes at about 250 cm⁻¹ for the $c(aa)\bar{c}$ polarization configuration. For the crossed $c(ab)\bar{c}$ polarization configuration (see Fig. 4) two Raman active B_{1g} symmetry modes at 91 and 177 cm⁻¹ are observed. Vertical bars in

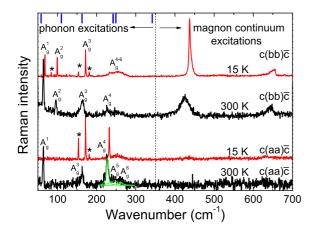


FIG. 3. (Color online) The (*aa*) and (*bb*) polarized Raman scattering spectra of BaFe₂Se₂O single crystals measured at room temperature and at 15 K. Vertical bars are calculated values of the A_g symmetry Raman active vibrations. Asterisks denote new Raman modes which appear at temperatures below $T_N = 240$ K.

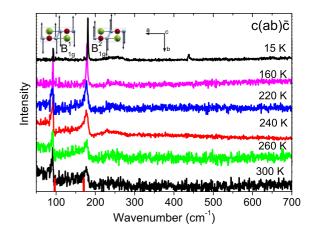


FIG. 4. (Color online) The (ab) polarized Raman scattering spectra of BaFe₂Se₂O single crystals measured at various temperatures between 15 and 300 K. Vertical bars are calculated values of the B_{1g} symmetry modes. Insets show the normal modes of the B_{1g}^1 and B_{1g}^2 symmetry Raman active vibrations, which originate from the Se and Fe atom vibrations along the *b* axis, respectively.

Figs. 3 and 4 denote the calculated energies of the A_g and B_{1g} symmetry mode, which are in rather good agreement with experimentally observed ones.

As we have shown in Fig. 2, the lowest energy A_g^1 mode is dominated by Ba atom vibrations along the c axis, the A_a^2 mode represents vibrations of Fe, Se, and O atoms which tend to rotate FeSe₃O chains around of the *b* axis. The A_{p}^{3} mode represents dominantly Se atom vibrations, whereas the A_g^4 mode originates dominantly from Fe atom vibrations. The A_{a}^{5} mode represents vibration of Fe atoms along the a axis together with vibrations of the oxygen atoms along the c axis. Finally, the A_a^6 mode originates from oxygen vibration along the c axis. Intensities of the last two modes are rather small as can be seen in Fig. 3, most probably because of oxygen deficiency in the sample. In fact, according to Mössbauer spectroscopy measurements³ about 8% of our sample shows FeSe₄ tetrahedral coordination of Fe ions instead of FeSe₃O. This suggest the possible presence of vacancies on the O site, excess Se and $BaFe_2Se_{2+\delta}O_{1-\delta}$ stoichiometry, which can alter intensity of oxygen related vibrational modes. Energies of the A_a^5 and A_a^6 modes are obtained from a broad structure peaked at about 250 cm⁻¹ using the Lorentzian line-shape deconvolution technique (see room temperature spectra for the (aa) polarization, Fig. 3).

By lowering the temperature A_g modes increase their energies and sharply reduce the linewidth below the phase transition temperature $T_N = 240$ K, as it is shown for the A_g^3 and A_g^4 modes in Fig. 5. Besides that signal-to-noise ratio in the Raman spectra measured at 15 K is significantly reduced by increasing the temperature to 300 K. We believe that this change is related to the spin ordering. In addition, new modes appear at temperatures below 240 K, most probably as a consequence of crystal structure and/or crystal symmetry change at T_N . These modes are denoted with asterisks in Fig. 3.

In addition to the phonon modes, two asymmetric structures are observed at about 425 and 645 cm⁻¹ at the roomtemperature Raman scattering spectrum for the $c(bb)\bar{c}$ polarization configuration only. These structures increase their

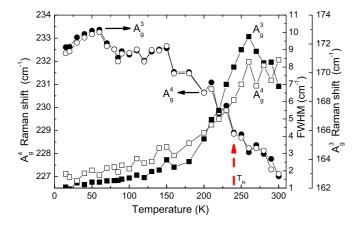


FIG. 5. (Color online) Energy (circles) and linewidth (squares) temperature dependence of the A_g^3 and A_e^4 symmetry modes.

intensity and harden substantially when the temperature is lowered, remaining asymmetric up to the lowest temperature of 15 K, see Fig. 6(a). Because the optical phonon region for the A_g symmetry modes is below 350 cm⁻¹ we assigned these modes as magnetic-ordering related for the following reasons:

(i) The magnetic susceptibility measurements⁴ show a broad peak between 400 and 500 K with a maximum around $T_{\text{max}} = 450$ K and an abrupt decrease towards zero at $T_N = 240$ K. This shape of the magnetic susceptibility is observed in many two-dimensional magnetic systems¹⁹ including the parent compounds of iron-based superconductors²⁰ and is connected to the short-range correlation of the local moments.²¹ The ratio of T_N/T_{max} is usually used to estimate the extent of the low-dimensional magnetic correlations.²² As T_N/T_{max} in BaFe₂Se₂O is 0.53, it can be concluded that BaFe₂Se₂O is a quasi-two-dimensional magnetic system, or more precisely a spin-ladder (dimer) system.

(ii) Magnon-related continuum appears only in the (*bb*) polarization, i.e., in the direction where the light polarization is collinear with spin orientation polarization.

(iii) In spin-ladder systems a triplet gap mode and a twomagnon continuum may appear in the Raman spectra.²³ As we already mentioned, the magnetic structure of BaFe₂Se₂O may be considered as the AFM spin-ladder (dimer) structure with a non-negligible interladder (dimer) interaction (strong Fe-O-Fe super-exchange interaction J_1 along the rungs of the S = 2 spin ladders is dominant; the interladder interaction J_2 is more than three times weaker than along the rungs⁴). Raman scattering spectra of the AFM dimer magnetic structure was a subject of our interest in Ref. 6, where we showed that the spin dimer structure in CaV_2O_5 is represented in the form of a two-magnon continuum with the singularities of the one-dimensional density of (two-magnon) states. In the case of BaFe₂Se₂O the two-magnon continuum is well separated from the A_g optical phonon range. The onset of the magnetic continuum appears at about 425 cm⁻¹ (437 cm⁻¹) at room temperature (15 K) as an asymmetric-shape line with a tail towards higher energies (M_0 critical point in the 1D density of magnon states). This continuum ends with the λ -shape line $(M_1 \text{ critical point in the 1D density of magnon states})$ peaked at about 645 cm⁻¹ (655 cm⁻¹) at room temperature (15 K). The total width of the continuum is estimated to be around

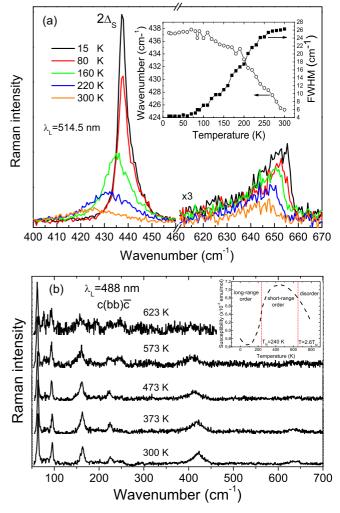


FIG. 6. (Color online) (a) The (*bb*) polarized Raman scattering spectra of BaFe₂Se₂O single crystals measured at various temperatures between 15 and 300 K in the 400–670 cm⁻¹ spectral range. Inset: Energy (circles) and linewidth (squares) of the $2\Delta_S$ (spin gap) mode as a function of temperature. (b) The same Raman spectra measured in the temperature range between 300 and 623 K. Inset: Magnetic susceptibility vs temperature from Ref. 4.

 230 cm^{-1} (15 K). The energy of the 437 cm⁻¹ line saturates at temperatures below 100 K, see the inset of Fig. 6.

(iv) The well-defined peak around $2\Delta_S$ is expected in the Raman spectra of the spin ladder (dimer), due to the singularities of the one-dimensional density of two-magnon states.⁶ Thus, we assigned the onset of the magnon continuum to $2\Delta_S = 437 \text{ cm}^{-1}$ (15 K) and obtain the spin gap in BaFe₂Se₂O to be 219 cm⁻¹ (27 meV).

(v) There is a common belief that the short-range magnetic order in oxychalcogenides extends at least up to temperature of $2T_N$.²² To check this assumption we have measured Raman spectra for the (*bb*) polarization at high temperatures up to 350°C (623 K). As can be seen from Fig. 6(b) the two-magnon continuum singularity modes decrease their intensity in comparison to phonon modes, and at temperature of about 623 K these modes completely disappear. Accordingly, we concluded that the short-range magnetic order in BaFe₂Se₂O persists up to about 2.6 T_N .

Finally, we believe that in the short-range order region [between T_N and $2.6T_N$, see the inset in Fig. 6(b)] there are also antiferromagnetic fluctuations of local magnetic moments. Spin fluctuations are coupled with the B_{1g} symmetry phonon modes. This coupling is manifested in the appearance of the B_{1g} mode line-shape asymmetry (the Fano-profile shape). Below T_N (see Fig. 4), this asymmetry vanishes as the system enters the long-range ordered antiferromagnetic state.

IV. CONCLUSION

We have measured the polarized Raman scattering spectra of the BaFe₂Se₂O single crystals at various temperatures. All Raman-active modes from the (*ab*) plane predicted by factor-group analysis have been experimentally observed and assigned. Frequencies of these modes are in rather good agreement with the lattice dynamics calculations. The A_g and B_{1g} mode linewidths and energies change substantially at temperatures below $T_N = 240$ K, where the system becomes antiferromagnetically long-range ordered. At frequencies higher than the A_{1g} optical phonon range we have observed a magnon continuum, which is related to the AFM dimer structure. The spin-gap value of 27 meV is obtained from

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the position of the onset of the magnetic continuum. Hightemperature Raman scattering measurements show that the short-range magnetic order disappears at about $2.6T_N$. In the short-range order region we have observed coupling of antiferromagnetic spin fluctuations with the B_{1g} symmetry phonons. It would be interesting to test and compare our results of the magnetic correlations with those of a low-temperature neutron scattering study of the BaFe₂Se₂O crystal, as well as theoretical calculations of magnon dispersions in the S = 2spin-ladder (dimer) barium iron oxyselenide compound.

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